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Survey on Optimal Ship Routing Algorithms: Enhancing Energy Efficiency and Operational Performance

Ch. Lakshmi Kumari¹*[†], J. RaviKiran²[†] and P. Komal Sai Charan³[†]

^{1,2,3}*Department of Information Technology, Mahatma Gandhi Institute of Technology, Gandipet, Hyderabad, 500075, Telangana, India. Corresponding author(s). E-mail(s): <u>1chlakshmikumari_it@mgit.ac.in</u>; Contributing authors: <u>2jravi_csb213223@mgit.ac.in</u>; <u>3pkomal_csb213248@mgit.ac.in</u>;

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ABSTRACT

Ship routing optimization has been the subject of extensive research due to the growing need for energy efficiency and emission reduction in marine trans- portation. The capacity of cutting-edge ship routing algorithms and strategies to enhance trip planning and execution while reducing fuel consumption, emissions, and operating expenses is the main emphasis of this survey. We offer a thorough analysis of the various routing technologies now in use, such as dynamic pro- gramming, machine learning, graph-based algorithms, and hybrid optimization strategies. Important factors like route accuracy, computing efficiency, weather- adaptability, and real-world implementation difficulties are examined. We also go over important elements that affect ship routing, like real-time data integra- tion, vessel performance, and environmental restrictions. The paper points out shortcomings in existing methods and emphasizes potential avenues for further research, such as the creation of real-time, adaptive routing algorithms that can handle uncertainty in changing maritime situations. The purpose of this paper is to provide scholars and practitioners in the field of marine logistics with a thor- ough resource that offers insights for creating cutting-edge ship routing solutions that guarantee sustainability and operational effectiveness.

Keywords: Ship Routing, Voyage Optimization, Dynamic Programming, Maritime Logistics, Fuel Efficiency, Machine Learning

1. Introduction

A key component of marine logistics is ship routing, which aims to maximize ship routes in order to limit fuel consumption, lower operating costs, and improve the effectiveness of international shipping operations. The intricacy of this work stems from elements that affect the selection of the best routes, including weather, ocean currents, navigational limitations, and fuel usage. Ensuring the sustainability and profitability of the shipping sector requires the development of an effective algorithm for optimal ship routing.Based on a number of factors, such as fuel consumption, time, and operational constraints, a ship routing algorithm determines the most effi- cient course for a vessel. Modern ship routing systems use optimization algorithms to determine dynamic, real-time routes that can adjust to changing conditions, whereas earlier methods have relied on manual planning and set routes. Route optimization techniques, which use mathematical models like linear programming, dynamic pro- gramming, and graph theory to determine the optimal ship routes, are among the most used methods [1].

Real-time weather forecasts, oceanographic data, and vessel-specific factors (such as cargo, speed, and fuel consumption rates) are examples of dynamic input data that an ideal ship routing algorithm should be able to manage. In addition to optimizing routes, these algorithms incorporate decision-making techniques that take operating economy, safety, and environmental effect into consideration. Ship routing systems are now able to process vast amounts of data and produce more accurate results thanks to developments in artificial intelligence (AI) and machine learning (ML) in recent years [2].Environmental factors are just as important as operational ones when it comes to ship routing efficiency. Optimizing ship routes can drastically cut fuel consumption and greenhouse gas emissions, which is important given the growing worries about climate change and the environmental effects of maritime transportation. As a result, there is now more interest in including environmental considerations in ship routing algorithms [3].

The objective of this study is to provide a flexible and quick algorithm for the best ship routing that takes environmental effects into account while balancing time, safety, and fuel efficiency. This program seeks to improve the overall efficiency and sustainability of maritime transportation by combining real-time data sources and applying sophisticated optimization techniques[4]. The global maritime sector, which accounts for more than 80% of all international trade by volume, is essential to the world's interdependent economies. At the core of this industry is effective ship routing, which has a direct impact on delivery schedules, operational costs, and envi- ronmental sustainability. A strong and flexible ship routing algorithm is necessary to handle the various issues that shipping operations encounter due to the increasing complexity of contemporary marine logistics[5].

In the past, ship routing relied on either static routes that were pre-established or manual planning. These methods, however, were not flexible enough to adjust to changes in the weather, ocean conditions, and operational needs in real time. These conventional approaches' drawbacks frequently led to less-

than-ideal routes, higher fuel consumption, and more expensive operating expenses[6]. The development of dynamic and intelligent ship routing algorithms that can process real-time data and produce adaptive solutions has become the main focus in response to these difficulties[7]. In order to optimize routes, contemporary ship routing systems make use of developments in computing techniques such as graph theory, dynamic pro- gramming, and linear programming. By analyzing a variety of variables, including vessel speed, cargo load, navigational restrictions, and environmental concerns, these mathematical models allow for accurate decision-making[8]. By enabling predictive modeling, data-driven optimization, and the capacity to learn from past trends, the integration of artificial intelligence (AI) and machine learning (ML) has further transformed ship routing[9].

Growing global awareness of climate change and the environmental impact of shipping operations has made environmental sustainability a crucial component of ship routing. Ship routing systems must reduce fuel usage and related emissions since the International Maritime Organization (IMO) has set aggressive goals for lowering greenhouse gas emissions from ships. Modern ship routing systems can support a more environmentally friendly marine sector while preserving economic viability by including environmental considerations into optimization algorithms[10]. A flexible and quick ship routing algorithm that strikes a compromise between environmental sustainability and operational efficiency is what the suggested study seeks to address. This program will offer dynamic routing solutions that adjust to shifting conditions by combining cutting-edge optimization techniques with real-time data sources, such as weather forecasts and oceanographic information. In order to guarantee that the produced system satisfies the various needs of the shipping industry, the study also places a strong emphasis on safety, time efficiency, and lower operating costs[11].

The complexities of ship routing, the use of sophisticated algorithms in maxi- mizing marine logistics, and the incorporation of environmental factors into routing choices will all be covered in this essay. Contributing to the creation of a technolog- ically sophisticated, efficient, and sustainable maritime transportation system is the ultimate objective[12].

1.1 An Overview of Ship Routing

The process of figuring out a vessel's safest and most effective route between two loca- tions while taking various goals and restrictions into consideration is known as ship routing. This area has a significant impact on delivery timetables, fuel consumption, operational expenses, and environmental sustainability in the maritime sector[13]. The main goals of optimal ship routing are essential for improving operational effectiveness and guaranteeing maritime navigation safety. By choosing energy-efficient routes, fuel optimization helps reduce fuel consumption, which is important for lowering operating costs and the impact on the environment. Another crucial factor to take into account is time efficiency, since meeting consumer requests and sustaining corporate operations depend on the timely delivery of passengers or supplies.

Ships must avoid dangerous places, such as areas vulnerable to severe weather, piracy hotspots, or shallow waters, which present serious threats to the ship and its crew. Safety is still of utmost importance. Because reducing carbon emissions and following international laws serve to lessen the environmental impact of the maritime industry, environmental compliance has grown in importance. Last but not least, a primary goal is dynamic flexibility, which allows ships to modify their courses in real time in response to shifting sea conditions, weather, or emergencies, guaranteeing that they can efficiently handle unforeseen situations and preserve operational effec- tiveness.

1.2 Challenges in Optimal Ship Routing

Ship routing optimization is a challenging issue that necessitates striking a balance between several goals and constraints[16]. In order to provide effective and secure vessel navigation, the marine sector must overcome several obstacles. To increase productivity, security, and environmental sustainability, optimal ship routing must overcome a number of obstacles. Sea conditions and weather are important factors; erratic weather patterns, including unexpected storms, typhoons, or changes in wind direction, might interfere with planned routes. Strong currents and high wave height can further lengthen journey times and increase fuel consumption, and traveling through polar regions increases the chance of running into icebergs and frozen waters. Cost and fuel efficiency are other important considerations, especially in light of the rising cost of fuel, which makes it imperative to select routes with the least amount of consumption. Furthermore, because it's difficult to strike a balance between meeting delivery dates and gasoline usage, the speed-fuel tradeoff is a recurring problem.

Routing options are further complicated by environmental constraints. In Emis- sion Control Areas (ECAs), ships are subject to more stringent emission regulations that necessitate fuel switching or route modifications. The operational complexity is further increased by international rules like IMO 2020, which requires fuels to have a lower sulfur content. Safety issues are similarly important; rerouting is necessary in pirate zones to avoid dangers, and precise mapping is necessary in shallow waters and navigational hazards to avoid grounding or crashes. Careful route planning is necessary since congested maritime routes raise the possibility of accidents. The opti- mization process may be hampered by technological constraints such as antiquated navigation systems and difficulties incorporating real-time data such as weather fore- casts, AIS data, and fuel metrics.

In dynamic scenarios that call for prompt rerouting, such engine problems, medi- cal emergencies, or abrupt weather changes, real-time route adjustments are essential. However, the prompt exchange of vital information may be impeded by inadequate connectivity at sea. Route options are also influenced by port and canal constraints, such as congestion, toll prices, and canal size restrictions (such as those in Panama or Suez), and delays at busy ports can offset time savings from optimal routes. Route design must take into account both operational and economic considerations, such as the requirement to manage crew tiredness and safety on lengthy voyages and strict delivery dates.

Ship routing is made even more difficult by environmental uncertainty. There are extra complications when avoiding ecologically delicate places like protected marine zones and coral reefs. Routing decisions become even more unpredictable due to seasonal variations, such as ice melts and monsoon

seasons. Last but not least, opti- mization algorithm difficulties need to be resolved because it takes a lot of computing power to create algorithms that effectively calculate the best routes while taking a lot of variables into account. The development of sophisticated ship routing systems is still hampered by the intricate decision-making procedures required to balance several goals, including cost, time, safety, and environmental impact.

1.3 Evolution of Routing Techniques

The maritime industry's growing demands for efficiency, safety, fuel optimization, and environmental sustainability have influenced the development of ship routing techniques. In the beginning, sailors plotted courses using manual instruments like compasses, sextants, and paper charts, depending on their expertise and experience. The precision and adaptability of these early techniques were constrained, especially when taking into consideration changing weather patterns or unforeseen barriers[31].

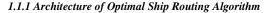
The first computer-based navigation systems appeared with the advent of com- puters in the middle of the 20th century, providing rudimentary aids for course planning. In order to determine the shortest distance between two sites, these early systems mostly used straightforward algorithms; they were unable to take into con- sideration dynamic elements like weather, fuel usage, or environmental dangers[32]. This signaled the start of the shift to more sophisticated ship routing techniques.

Optimization algorithms like Dijkstra's algorithm and dynamic programming became more well-known in the 1970s and 1980s. By taking into account variables like speed, safety, and fuel efficiency, these algorithms made it possible to plan routes in a more complex way. The advent of satellite communication and real-time weather data allowed ships to dynamically modify their courses in order to steer clear of storms or choppy waters[33]. Although these systems were still mostly reactive and reliant on predetermined conditions, fuel usage started to be taken into account when making routing decisions, particularly as fuel prices increased.

Heuristic and metaheuristic algorithms, such as Genetic Algorithms (GA), Sim- ulated Annealing (SA), and Ant Colony Optimization (ACO), emerged in the 1990s and 2000s and offered increasingly sophisticated solutions to routing issues. These techniques could take into consideration several goals, such reducing fuel consumption while adhering to deadlines and averting dangers. More dynamic decision-making was made possible by the incorporation of real-time data from sources like as Automatic Identification Systems (AIS), and the systems started to manage several vessels simultaneously[34]. The computational difficulties of planning routes for entire fleets and the intricacy of integrating big databases, however, continued to be major barri- ers.

Artificial intelligence and machine learning transformed ship routing in the 2010s and beyond. In order to more accurately forecast and optimize routes, artificial intelligence (AI) systems now examine enormous information from numerous sources, such as historical weather data, ship performance indicators, and environmental variables[35]. Real-time hazard avoidance is made possible by predictive analytics, and real-time information on engine performance, fuel consumption, and other aspects is obtained by interaction with IoT devices on ships. An important turning point in this history has been reached with the creation of autonomous and semi-autonomous ships, which can make real-time routing decisions without human assistance, lowering the possibility of human error and improving safety.

More cooperation between ships is anticipated in the future of ship routing, as fleets exchange real-time data to jointly optimize routes and cut emissions and fuel usage. Blockchain technology has the potential to improve data security and transparency while maintaining the accuracy of routing data. Routing systems will increasingly concentrate on reducing the environmental impact of maritime opera- tions as sustainability gains traction. This will involve implementing low-emission routes and more stringent adherence to environmental rules. Ship routing's transition from manual to AI-driven, autonomous systems exemplifies how the marine sector is constantly changing as technology advances efficiency, sustainability, and safety[36].



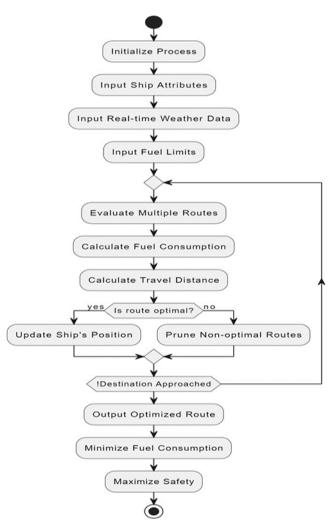


Fig. 1 Architecture of Optimal Ship Routing Algorithm

A process for an ideal ship routing system is shown in Figure 1. The first step in the procedure is gathering input data, such as sea conditions, current weather fore- casts, and vessel characteristics. The correctness and completeness of this material have been confirmed. The user is prompted by the system to re-enter the necessary information if any of the input data is missing or incorrect. In order to maintain efficiency and safety, the system can provide real-time updates in response to shifting circumstances, such as unexpected weather shifts or emergency situations. Addition- ally, it verifies adherence to global marine laws.

1.2 Objective and Scope of the Study

The study's main goal is to create a flexible and effective algorithm for ship routing that minimizes fuel consumption, lowers operating expenses, and optimizes route selection depending on a number of factors. To find the best path for ships, the computer will consider variables like fuel economy, course possibilities, weather, and geographic restrictions. The project aims to improve ship routing systems' accuracy and processing speed by applying sophisticated decision-making approaches, such as optimization algorithms and pruning procedures, which would result in more eco- nomical, secure, and ecologically friendly marine operations.

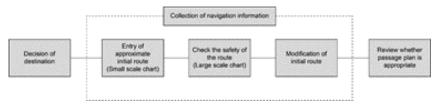


Fig. 2 Navigators Route Planning Process

The study's scope includes optimization criteria that give time, operational effectiveness, and fuel consumption top priority. A balance between speed, fuel effi- ciency, and safety will be achieved by taking into account variables such as weather patterns, sea currents, and geographical barriers. The computer will evaluate the environmental effects and recommend the best routes between departure places and destinations, avoiding obstructions like reefs or shipping channels. The algorithm's speed and accuracy will increase as non-optimal paths are removed through the use of pruning strategies. Additionally, by taking into consideration changing maritime cir- cumstances, real-time weather data integration will improve route recommendations.

The algorithm's ability to lower fuel consumption, operational expenses, and tran- sit time while maintaining the ship's dependability and safety will be the basis for the study's evaluation of its efficacy. To make sure the algorithm balances processing time and accuracy, computational efficiency will also be prioritized. By connecting with current fleet management systems, the algorithm will work with both commercial and cargo ships and may even be used with military or research vessels. Geographically, the study will concentrate on international shipping lanes, taking into account the particular difficulties of traveling via various locales, such as high-traffic zones or the Arctic. The study's ultimate goal is to aid in the creation of more intelligent and environmentally friendly ship routing systems for the marine sector.

1.2.1 Traditional Ship Routing Mechanisms

The term "traditional ship routing mechanisms" describes the procedures and approaches that were formerly employed to find the best routes for ships based on predetermined parameters, including time, distance, or fuel consumption, frequently without taking into account dynamic or real-time environmental data. To plan and guide ship voyages, these algorithms mostly used static inputs like maps, pre- established routes, and basic mathematical models.

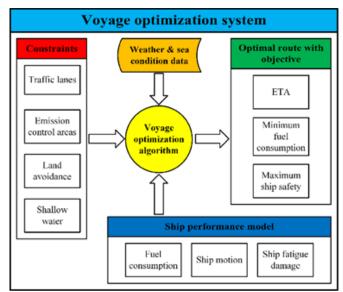


Fig. 3 Voyage Mechanism

A) Classical Optimization Mechanisms

Ship routing has traditionally employed traditional methods like graph theory, dynamic programming, and linear programming (LP). For issues with linear restric- tions, like maximizing fuel efficiency for a specific route or reducing travel time under predetermined circumstances, linear programming works especially well. More complicated issues with several decision points over time, including ship routing optimization in the face of shifting ocean currents or weather conditions, are handled via dynamic programming. The voyage of the ship is represented as a graph by graph theory approaches, in which every port or waypoint is a node and the connections between them are edges. In these situations, algorithms such as Dijkstra's algorithm and A algorithm* are frequently used to find the quickest or most economical routes based on a variety of factors. For large-scale problems, these approaches necessitate substantial computer resources and frequently struggle with real-time flexibility[13].

B) Heuristic Mechanisms

Heuristic techniques like simulated annealing (SA), ant colony optimization (ACO), and genetic algorithms (GA) have become more and more popular for resolving ship routing issues with large and intricate search spaces. These algorithms are especially helpful when there are several goals involved, including balancing time, safety, and fuel efficiency, and when precise solutions might not be computationally possible. In order to investigate many routing alternatives and converge towards an ideal solution, genetic algorithms mimic natural evolutionary processes including selec- tion, crossover, and mutation. Through the use of pheromone trails, artificial "ants" navigate possible routes and exchange information about the best routes, simulating the behavior of ants in search of food. Both of these methods work well in dynamic settings where decision-making requires the integration of real-time weather and oceanographic data. Nevertheless, these methods can be computationally demanding and could not always provide the global optimum[20].

C) Artificial Intelligence and Machine Learning Approaches

Ship routing algorithms are now far more accurate and flexible thanks to recent developments in artificial intelligence (AI) and machine learning (ML). Artificial intel- ligence (AI)-based methods, including reinforcement learning (RL), are very useful for dynamic and real-time optimization because they enable systems to continuously learn from their surroundings. In reinforcement learning (RL), the algorithm repeat- edly performs different actions and learns to choose the optimal one based on rewards (e.g., limiting fuel usage or avoiding poor weather). Additionally, compared to conventional techniques, neural networks can be trained to forecast the best routes based on past data and environmental inputs, yielding more precise and dependable results. To continuously adjust and improve routing choices, deep learning models can also be combined with real-time data sources such as ship specs, ocean currents, and satel- lite weather reports[7]. Although these AI-driven approaches frequently need a large amount of data and computer power, they are quite successful at solving complicated, multifaceted problems.

D) Hybrid Approaches

To capitalize on each algorithm's advantages, academics and practitioners occasion- ally combine several algorithms. For instance, a hybrid strategy might combine the flexibility of AI techniques with the computing effectiveness of traditional optimiza- tion methods. These hybrid systems can optimize for several factors while adapting dynamically to shifting conditions (such as weather or fuel consumption)[16]. Since these methods may strike a balance between precision, flexibility, and computing econ- omy, they are being more and more regarded as potential solutions for the maritime sector.

2. Feature Extraction

Finding the crucial factors that affect the routing decision-making process is the goal of feature extraction in the creation of an ideal ship routing algorithm. These aspects, which affect the routing algorithm's effectiveness, safety, and economy, include weather, ship attributes, route parameters, and fuel usage considerations.

2.1 Weather conditions

One of the biggest determinants of the best ship routing is the weather. The ship's speed and fuel usage are greatly impacted by the wind's direction and speed. While favorable winds can help cut down on journey time and fuel requirements, high winds can cause the ship to slow down and use more fuel. Because severe seas can result in slower speeds and higher fuel consumption, the sea state—which includes wave height, frequency, and direction—also plays a significant effect. Similar to this, current direction and speed must be taken into account because ocean currents can either help or hinder a ship's progress, which affects fuel economy. Furthermore, visibility and fog conditions might affect safety and route choices, particularly in crowded or poorly charted locations.

2.2 Ship characteristics

When figuring out the best course, ship attributes are just as crucial. The operational speeds and fuel economy of a ship are determined by its kind, such as tankers, bulk carriers, or container ships. Generally speaking, larger ships use more fuel and may be subject to more stringent restrictions on the routes they can travel, particularly with regard to draft and width. Because it impacts maneuverability and the ship's capacity to travel through shallow or narrow seas, the algorithm must take into account the ship's dimensions, including its length, beam, and draft. The best cruising speed and fuel consumption are determined in large part by engine efficiency, which also affects the selection of routes and speeds.

2.3 Route parameters

Important variables like distance—the total distance traveled between the start- ing point and the final destination, including any detours or alternate routes—are included in the route parameters. Shipping firms are frequently subject to time con- straints in order to fulfill delivery dates. The trade-off between fuel usage and travel speed may be impacted by these time-sensitive demands. Because port delays might affect the entire routing plan, it is also important to take into account the closeness to port locations and possible port congestion. Additionally, the ship's speed and route decisions may be impacted by the volume of traffic in maritime lanes. Routes that cross crowded shipping channels might need to be modified to avoid collisions or move more slowly[29].

2.4 Fuel consumption

Environmental emissions and operating costs are directly impacted by the type of fuel utilized, such as diesel, LNG, or heavy fuel oil. The choice of routes to cut costs might be influenced by regional variations in gasoline prices. To maximize both cost and fuel efficiency, the bunker consumption rate—which is the amount of fuel used per unit of distance at different speeds—should also be taken into account. Together, these elements serve as the basis for creating a ship routing algorithm that optimizes performance in a variety of operational scenarios by striking a balance between speed, fuel economy, safety, and cost-effectiveness.

Numerous sophisticated methods are applied, each concentrating on a distinct facet of the routing issue. While A algorithm* is excellent at determining the best course based on time, fuel consumption, and sea conditions using a heuristic approach, algorithms such as Artificial Neural Networks (ANN) use historical data and environmental variables to forecast ideal routes. When preliminary estimates are not provided, Dijkstra's Algorithm is dependable for routing because it guarantees thorough route evaluation, taking into account every potential path to identify the least expensive option. Furthermore, in

order to evolve and optimize routes based on multi-objective criteria including fuel efficiency, distance, and time, Genetic Algorithms (GA) and Particle Swarm Optimization (PSO) employ evolutionary and swarm-based concepts, respectively.

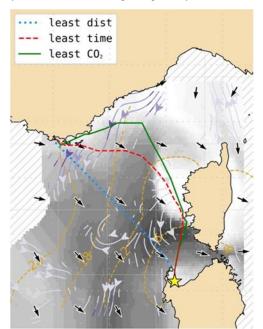


Fig. 4 Optimising routes by considering features

Given the dynamic nature of maritime navigation, each algorithm has unique ben- efits. By avoiding local minima, the probabilistic methodology of Simulated Annealing (SA) facilitates the exploration of a large solution space and the discovery of globally optimal solutions. When incorporated into an all-encompassing ship routing system, these algorithms guarantee more effective, flexible, and ecologically responsible vessel navigation choices. These methods give decision-makers the means to optimize routes for sustainability and cost-effectiveness, which eventually improves operational performance in the maritime sector. They do this by taking into account variables such as fuel consumption, ship characteristics, and current environmental conditions.

3. Review of Literature

A thorough examination of the benefits and drawbacks of the primary real-time open source algorithms utilized in everyday life is provided, along with information on their methods and mechanisms.

3.1 Artificial Neural Networks (ANN) in Ship Routing

The capacity of Artificial Neural Networks (ANNs) to represent intricate, nonlinear relationships between input data and decision outcomes has led to an increase in their application in ship routing optimization. In order to anticipate the most effective routes, ANN-based ship routing algorithms usually use historical data as well as envi- ronmental factors like wind speed, ocean currents, and sea condition. These networks are useful for real-time route optimization in dynamic maritime situations because they can adapt over time and learn from vast datasets. According to research, arti- ficial neural networks (ANNs) can accurately anticipate ship itineraries that reduce fuel usage while taking unpredictably occurring environmental elements into account.

3.2 A* Algorithm in Ship Routing

Another efficient technique for ship routing is the A* algorithm, which is frequently used in pathfinding and graph traversal. Based on a heuristic approach, this program strikes a balance between using known efficient paths and exploring potential routes. It makes use of a cost function that determines the most cost-effective route by taking into account factors like distance, fuel consumption, and sea conditions. A* may be tailored to ship routing to take time, fuel, and safety considerations into account, ensuring optimal navigation in a variety of sea conditions. It is particularly useful in limited contexts where real-time decision-making is crucial.

3.3 Dijkstra's Algorithm in Ship Routing

A popular graph search algorithm for determining the shortest routes between nodes in a graph is Dijkstra's Algorithm. Ship routing has employed this algorithm to reduce fuel consumption and journey time. Dijkstra's Algorithm, in contrast to A*, takes into account every route that could go from the

starting point to the destination and assesses each one using predetermined cost metrics, such time and fuel consumption. Even in cases where the initial conditions are unclear or insufficient, our thorough technique guarantees that the best path is selected. When dealing with huge datasets or changing situations, Dijkstra's Algorithm can be computationally costly, but it is especially helpful when taking into account different paths and conditions.

3.4 Genetic Algorithm (GA) in Ship Routing

Natural selection serves as the inspiration for Genetic Algorithms (GA), which are evolutionary algorithms used in ship routing to maximize multiobjective problems. These algorithms mimic the selection, crossing, and mutation of solutions (routes) to create better solutions over the course of multiple generations, simulating the process of evolution. GA can optimize ship routes by taking into account a number of variables, including speed, fuel consumption, and environmental conditions. GA's capacity to manage several goals at once makes it appropriate for adaptive routing and real-time decision-making, where several aspects are evaluated and optimized.

3.5 Particle Swarm Optimization (PSO) in Ship Routing

The population-based optimization method known as Particle Swarm Optimization (PSO) was motivated by the social behavior of fish schools and flocks of birds. PSO employs a swarm of particles (possible routes) to navigate the solution space in ship routing. These particles are guided by their own experiences as well as those of their neighbors. As particles adjust their positions in response to the best solutions discovered by themselves and their neighbors, the swarm converges towards the ideal solution. PSO has been used to ship routing for multi-objective optimization, offering methods that optimize for time, safety, and environmental factors while consuming the least amount of fuel. Its simplicity and effectiveness in examining vast, intricate solution spaces are its main advantages.

3.6 Simulated Annealing (SA) in Ship Routing

The annealing process in metallurgy, in which the system progressively cools to a stable condition, served as the model for the probabilistic technique known as Simu- lated Annealing (SA). By probabilistically tolerating less optimum routes at first and progressively concentrating on better solutions over time, SA is used in ship rout- ing to explore a large solution space and locate an ideal or nearly optimal solution. By avoiding local minima, this method guarantees the discovery of global optimal routes. SA is appropriate for dynamic ship routing scenarios with unpredictable and variable climatic conditions because it is especially good at solving huge, compli- cated routing issues where exhaustive search techniques like Dijkstra's or A* might be computationally impractical[33].

Literature Table

Table 1 Literature Table

Title	Author	Journal Name Year	&Methodology Adapted	Key Findings	Gaps
A Ship	Yuankui Li,	Journal of	Customized 3D	Enhanced	Did not
Route	Jinlong Cui,	Marine	A* algorithm,	navigational	consider specific
Planning	Xinyu Zhang	Science and	ship course and	safety and	environmental
Method		Engineering,	speed	efficiency,	complexities like
under the		2024	optimization,	reduced fuel	ocean currents
Sailing Time			rasterized	consumption	or ice-covered
Constraint			dynamic sea	compared to	waters; ANN's
			area model,	historical routes,	fuel
			artificial neural	avoided adverse	consumption
			network (ANN)	sea conditions,	prediction
			for fuel	and ensured	model could be
			consumption	ship arrival close	further refined.
			prediction	to the estimated	
				time of arrival.	

A Mathe-	Lili Huang	Journal of	Ant colony	Ant colony	Did not account
matical		Mathematics	algorithm,	algorithm	for real-world
Modeling		Volume,	MATLAB	achieved fewer	complexities
and an		2023	simulation	iterations,	such as dynamic
Optimization			environment,	shorter	environmental
Algorithm			comparison with	optimization	conditions,
for Marine			AI and genetic	times, better	obstacle
Ship Route			algorithms	success rate in	variations, and
Planning				route planning,	changing
				and reduced	weather
				path lengths.	patterns.
Artificial	Cem	Journal of	Surrogate model	Significantly	Did not account
Neural	Guzelbulut,	Marine	combining	reduced energy	for time-varying
Network-	Timoteo	Science and	artificial neural	consumption by	environmental
Based Route	Badalotti,	Engineering,	networks and	navigating	conditions.
Optimization	Yasuaki	2024	MMG ship	through	
of a Wind-	Fujita		dynamics model	low-wind speed	
Assisted			for energy	areas and	
Ship			consumption	optimizing rotor	
			and route	sail utilization.	
			optimization		

Table 2 (Continued) Literature Table

Title	Author	Journal Name	& Methodology	Key Findings	Gaps
		Year	Adapted		
Safety	Tae-eun	WMU	Hazard analysis	Emphasized the	Limited research
challenges	Kim,	Journal of	approach,	need for	on cooperative
related to	Lokukaluge	Maritime	Systems	cooperative	navigation
autonomous	Prasad	Affairs, 2022	Theoretic	navigation,	between
ships in	Perera		Process Analysis	secured	autonomous and
mixed			(STPA) for	communication,	conventional
navigational			identifying	and hazard	vessels; need for
environ-			potential risks	analysis to	more systemic
ments				safely integrate	approaches to
				autonomous	hazard analysis.
				vessels in mixed	
				environments.	
Modification	Alex Topaj,	International	Modification of	Successfully	Simplifications

of ship	Oleg	Conference	graph-based and	identified	like basic
routing	Tarovik,	on Port and	wave-based	optimal routes	integration and
algorithms	Andrey A.	Ocean	pathfinding	using local weak	limited
for the case	Bakharev	Engineering	methods for	ice areas,	icebreaking
of navigation		under Arctic	optimizing ship	minimizing	resources; key
in ice		Conditions,	routing in ice-	travel time and	challenge in
		2019	covered waters,	fuel	accessing
			incorporating	consumption,	quality, up-to-
			icebreaker	with routes	date weather
			assistance and	varying when	and ice data.
			ice condition	icebreaker	
			data.	assistance was	
				available.	
Multi-	Marcin	Polish	Multi-objective	Considering	The current
Objective	Zyczkowsk,	Maritime	deterministic	comfort criteria	model lacks a
Weather	Rafal	Research,	weather routing	extends routes	detailed
Routing of	Szlapczynski	2017 Vol. 24	method,	and voyage	representation
Sailing			customizable	times, while	of vessel
Vessels			criteria,	dynamic	dynamics, which
			dynamic	forecasts yield	limits accuracy,
			weather data,	different paths,	and further
			SailingAssis-	showcasing the	research is
			tance	method's	needed to
			application	adaptability to	improve this
				user	aspect.
				preferences.	

Table 3 (Continued) Literature Table

Title	Author	Journal Name Year	&Methodology Adapted	Key Findings	Gaps
A compre-	Manel	Ocean	A* algorithm	Time savings	The study lacks
hensive ship	Grifoll,	Engineering,	for ship route	ranged from	regional
weather	Clara Bor´en,	2022	optimization,	0.61% to 28.69%	specificity for
routing	Marcella		real-time wave	across global	the Indian
system using	Castells		data from	test cases. The	Ocean and does
CMEMS	Sanabra		CMEMS,	A* algorithm	not account for
products and			Python	provided	ship-specific
A* algorithm			visualization	efficient routes	attributes like

		and analysis	while	drift
			minimizing	characteristics.
			emissions and	entitudeenisties.
Debabrata	Applied	Modified version		A detailed
			_	comparison
			-	between
		-		methods is
rauly	2015	-		
				lacking due to
				the proprietary
				nature of some
		-	-	algorithms.
		,		Practical usage
		L		by ship
		examples		navigators
			and adaptability	remains unclear,
			to different sea	with limited
			conditions.	application
				onboard.
Artemis	8th	High-resolution	Satellite-derived	The literature
Ioannou,	International	oceanic current	HIRES currents	focuses heavily
Evangelos	Symposium	data from	outperform	on fuel
Moschos,	on Ship	satellite	traditional	consumption
Briac Le Vu,	Operations,	observations,	ocean models,	and
Alexandre	Management	artificial	reducing	decarbonization,
Stegner	& Economics	intelligence	prediction	while the
	(SOME),	processing,	errors.	project
	March 2023,	comparison with	Optimized	emphasizes a
	Athens,	traditional	routes resulted	multi-parameter
	Greece	operational	in fuel savings	Approach considering
		oceanic models	of 3-5% and	Passenger comfort
				safety, and voyage time.
			time reductions	
	Ioannou, Evangelos Moschos, Briac Le Vu, Alexandre	Sen andOceanChinmaya P.Research,Padhy2015Padhy2015ArtemisSthIoannou,InternationalEvangelosSymposiumMoschos,on ShipBriac Le Vu,Operations,AlexandreManagementStegner& Economics(SOME),March 2023,Athens,	Sen andOceanof Dijkstra'sChinmaya P.Research,algorithm,Padhy2015optimizationmodel forminimum-timeroute,3rd-generationWAM model,practicalpracticalexamplesArtemis8thHigh-resolutionIoannou,Internationaloceanic currentEvangelosSymposiumdata fromMoschos,on ShipsatelliteBriac Le Vu,Operations,observations,AlexandreManagementartificialStegner& Economicsintelligence(SOME),processing,march 2023,Athens,traditionaloperational	Sen andOceanof Dijkstra'sefficientlyChinmaya P.Research,algorithm,determinesPadhy2015optimizationminimum-timeModel forsea routes in theminimum-timeNorth Indianroute,Ocean by3rd-generationaccounting forWAM model,practicalpracticalconstraints,exampleswith versatilityand adaptabilityto different seaconditions.optimicationIoannou,InternationalDoeanou,InternationalBriac Le Vu,Operations,Stegner& EconomicsAlexandreManagementArtemisKeconomicsmoschos,or Shipstegner& EconomicsMarch 2023,comparison withOptimizedAthens,raditionaloptimizedficialroutes resultedficialintelligenceprotesting,errors.March 2023,comparison withoptimizedAthens,ficielin fuel savings

 Table 4 (Continued) Literature Table

Title	Author	Journal Name & Year	Methodology Adapted	Key Findings	Gaps
Risk	Juan-Chen	Journal of	AIS data for	AIS data is used	Focus is on
Assessment	Huang,	Marine	anomaly	for anomaly	constrained
and Traffic	Shuen-Tai	Science and	detection and	detection,	maritime areas,
Behaviour	Ung	Engineering,	ship behavior	collision	with limited
Evaluation of		2023	assessment,	avoidance, and	mention of
Ships			machine	behavioral	optimizing
			learning, deep	prediction. Deep	routing for
			learning,	learning	larger, less
			clustering	methods predict	constrained
			techniques like	future ship	oceanic routes
			DTW and	movements and	like the Indian
			density-based	risks, aiding in	Ocean. No
			spatial	optimized	explicit focus on
			clustering	navigation.	real-time fuel
					optimization.
Multi-	Jicheng	Journal of	IMACO	Routes differ for	The IMACO
Objective	Yang, Letian	Marine	algorithm	different	algorithm does
Weather	Wu, Jian	Science and	combined with	shipping	not account for
Routing	Zheng	Engineering	TOPSIS	companies due	live updates, a
Algorithm		(JMSE),	method, grid	to varying risk	critical feature
for Ships:		2022	method for	management	in dynamic
The			marine	and fuel	route
Perspective			environment	efficiency	adjustments.
of Shipping			modeling,	strategies. The	The project
Company's			evaluation of	IMACO	tailors the
Navigation			fuel	algorithm	optimization for
Strategy			consumption	outperforms	the Indian
			and navigation	single-objective	Ocean, while
			risks	algorithms in	the literature
				optimizing	provides a
				safety and fuel	general global
				costs.	solution.

4. Evaluation Metrics

To make sure an ideal ship routing algorithm lowers fuel consumption, cuts down on journey time, and improves safety and comfort, it is crucial to assess its efficacy. Automated evaluation indicators are typically applied, including fuel consumption reduction, time savings, and emission reductions. By lowering fuel use and cutting down on travel time while accounting for environmental factors, these measurements aid in evaluating how well the algorithm optimizes routes[16]. In this situation, the F-measure is a useful tool because it balances precision and recall to assess the algor- rithm's effectiveness in terms of route optimization and fuel efficiency. Additionally, the algorithm's capacity to identify the most efficient pathways under dynamic set- tings is validated by comparing its output to real-world or simulated scenarios.

Comfort and safety are important factors in human-based evaluations. The skill of navigators or other maritime professionals is used to evaluate these criteria, determin- ing how well the algorithm incorporates user choices pertaining to passenger comfort and safety. The practical usability of the algorithm in actual marine operations is determined by these evaluations, which are essential. The algorithm's capacity to adjust to changing sea conditions can also be improved by combining deep learning methods with real-time weather data. Furthermore, in order to handle unforeseen difficulties like weather variations and ocean currents, an algorithm that provides dynamic adjustments based on real-time data is essential[23].

Furthermore, scalability and flexibility to various maritime regions and situations are important considerations when assessing an optimal ship routing algorithm. The algorithm's adaptability is further enhanced by its capacity to manage a variety of maritime conditions, including the Indian Ocean, which has distinct currents, wave heights, and weather patterns. For example, algorithms can increase route accuracy and fuel efficiency by using real-time oceanic currents, such as those obtained from satellite observations, and dynamic meteorological data. The algorithm's ability to optimize routes across diverse geographies with changing sea conditions is ensured by testing it in multiple geographical locations, offering a more reliable ship navigation solution.

Finally, a crucial element in determining the routing algorithm's effectiveness is the assessment of safety and risk management. Potential dangers, including as collision risks, piracy, and other maritime concerns, must be recognized and mitigated by the algorithm. The program can monitor vessel behavior and notify operators of unusual activity by incorporating real-time data, such as Automatic Identification System (AIS) information, improving the safety of the journey. Assessing the algorithm's capacity to anticipate and steer clear of such hazards helps guarantee that it is not merely effective but also dependable and safe. An ideal ship routing system is built on the foundation of efficiency, adaptability, and safety, which is why continuing review is a crucial component of ongoing advancements in marine navigation technology[24].

5. Discussion

Through increased route efficiency, cost savings, and environmental sustainability, the creation of algorithms for efficient ship routing has fundamentally changed maritime operations. Advanced optimization algorithms that take into account dynamic aspects like weather patterns, sea currents, and vessel characteristics have outperformed tra- ditional ship routing methods, which mostly depended on static inputs like time and distance. Ship routing systems are now more accurate and flexible thanks to these developments, which provide better decision-making and increased operational effec- tiveness. However, there are issues with data availability, processing demands, and integrating real-time information when implementing such complex algorithms[32].

Heuristic algorithms, evolutionary tactics, and artificial intelligence are some of the methods used by contemporary ship routing systems to optimize routes. Route planning has been transformed by the combination of real-time geographic data and weather prediction algorithms, which allow ships to avoid unfavorable conditions and use less fuel. Even with these advancements, resource-intensive models still need large datasets and a lot of processing power to work well. This emphasizes that in order to get over these restrictions, computer power and data collection techniques must be continuously improved. Furthermore, handling sparse data and complicated decision-making situations is still difficult, requiring scalable algorithms and strong data processing frameworks[34]. The best ship routes have been found using optimiza- tion techniques including pruning and hybrid approaches that combine many machine learning and deep learning models. By removing less-than-ideal solutions early on, these techniques lower computing overhead. Cutting-edge methods that adjust to changing maritime conditions, such as metaheuristic algorithms and reinforcement learning, further improve decision-making. Despite their potential, these methods' high computational and training time requirements prevent their widespread use.

Ship routing algorithms are now more situationally aware thanks to the integration of Geographic Information Systems (GIS), real-time Automatic Identification System (AIS) data, and environmental monitoring systems. Multi-objective optimization is one technique that makes it possible to balance competing factors like safety, transit time, and fuel efficiency. Significant obstacles are presented by these sophisticated systems' high implementation costs and reliance on real-time, high-quality data. Some of these limitations can be removed by implementing parallel processing frameworks and cloud-based computing, which will increase the scalability and accessibility of ship routing solutions.

A dynamic interaction between contemporary computational developments and traditional nautical expertise is reflected in the growth of optimal ship routing sys- tems. The earliest approaches, which concentrated on shortest-path algorithms, have developed into complex models that can take into account multiple dimensions. In response to the increased need for environmentally friendly shipping methods, these developments seek to strike a delicate balance between economic feasibility and

environmental sustainability. Future developments in this area will probably concen- trate on combining cutting-edge technology for safe and effective data sharing, like blockchain, predictive analytics, and autonomous navigation.

In conclusion, the creation of optimal ship routing algorithms is the result of a fusion of state-of-the-art computational methods and conventional maritime pro- cedures. The ongoing development of optimization techniques and computational skills holds promise for the creation of effective, sustainable, and adaptable ship routing systems, despite ongoing obstacles including high computational costs, data limitations, and complex decision-making. These developments support international initiatives for resource optimization and environmental preservation in addition to the maritime sector[36].

6. Conclusion and Future Work

The creation of algorithms for the best ship routing has significantly improved mar- itime operations by lowering transit times, increasing fuel economy, and encouraging ecologically friendly behavior. Modern ship routing systems are more accurate and flexible than traditional methods thanks to the integration of real-time data, dynamic weather conditions, and sophisticated optimization techniques. These systems have proven their capacity to handle difficulties including scant data and computational resource requirements while striking a balance between several goals, including cost- effectiveness, safety, and environmental impact.

Effective route planning has been made possible by the use of strategies including hybrid machine learning models, multi-objective optimization, and pruning tech- niques, which have improved the decision-making process. Resource limitations, high implementation costs, and the difficulty of managing changeable maritime settings continue to be problems, nevertheless. Notwithstanding these challenges, the progress made thus far demonstrates the revolutionary potential of contemporary algorithms in ship route optimization for a variety of applications.

6.1 Future Work

The future of optimal ship routing algorithms lies in overcoming current limitations and leveraging emerging technologies to enhance their efficiency, scalability, and appli- cability. A primary focus will be the integration of autonomous navigation systems, allowing real-time, self-optimizing route adjustments with minimal human interven- tion, thereby improving operational efficiency. Advances in big data analytics and environmental monitoring will enable richer datasets, enhancing model accuracy and adaptability to dynamic maritime conditions.

Computational innovations such as cloud computing, parallel processing, and the potential of quantum computing are poised to address resource constraints, making sophisticated algorithms more accessible. Sustainability will also play a central role, with future algorithms incorporating metrics for carbon emissions and alternative fuels to align with global green shipping initiatives. Expanding the scope to multi-modal optimization, including connections with ports and inland logistics, will facilitate end- to-end supply chain efficiency.

The development of adaptive learning models, particularly through reinforcement learning, will allow systems to improve continuously with new data, enhancing robust- ness. Additionally, blockchain technology could secure data sharing across vessels, ports, and monitoring systems, fostering trust and collaboration within the industry. Efforts to optimize routing for low-resource regions, where data and computational infrastructure are limited, will further broaden the global impact of these systems. By addressing these areas, future advancements in ship routing algorithms promise to rev- olutionize maritime operations, contributing to economic efficiency and environmental sustainability on a global scale.

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