



## **Shedding Light on Rare Earths: A Spectroscopic Odyssey into Diverse Transitions**

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### **ABSTRACT**

Rare earths, a group of elements renowned for their unique optical and electronic properties, play pivotal roles in various technological applications. This review critically evaluates and consolidates the current state of knowledge concerning the application of spectroscopy to unravel the diverse transitions exhibited by rare earths. Commencing with an overview of the industrial significance of rare earth elements, the review delves into an exhaustive examination of spectroscopic methodologies. Classical techniques such as absorption spectroscopy and luminescence spectroscopy are scrutinized alongside state-of-the-art approaches, including magnetic resonance spectroscopy. Each method is comprehensively analyzed for its underlying principles, strengths, and limitations, providing readers with a nuanced understanding of the spectroscopic arsenal available for rare earth investigations. Furthermore, the review spotlights recent advancements and innovative applications of spectroscopy in deciphering rare earth transitions. By presenting examples of specific rare earth compounds and materials, the article illustrates the practical implications of spectroscopic interventions, emphasizing their role in understanding and optimizing the unique properties of these elements for diverse technological advancements. This review not only synthesizes existing knowledge but also stimulates further exploration, inspiring researchers to embark on new frontiers in rare earth spectroscopy.

Keywords: Rare Earths, Luminescence, Emission, Transition, Applications

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### **1. Introduction**

The study of rare earth elements has evolved as a fascinating and important area within the realm of materials science. This is mostly due to the unique electrical and optical properties that are demonstrated by this group of elements. There are a multitude of applications in the fields of electronics, telecommunications, energy, and other areas that are at the forefront of this investigation. Each of these applications makes use of the distinctive qualities that rare earths possess. The complexity of these elements, which are distinguished by their intricate electronic structures and various oxidation states, have prompted a significant research attempt to decipher the behavior of these elements. From a historical point of view, the lanthanide series, which includes scandium and yttrium, as well as the rare earth elements, have been a source of fascination for scientists and engineers ever since their discovery in the late 18th century. Due to the fact that many of these elements are not particularly uncommon, the name "rare earths" might be somewhat deceptive. This is because the chemical similarities between these elements make it difficult to extract and refine them further. The early applications of rare earths were primarily focused on their colorful luminescence qualities. Elements such as europium and terbium were utilized in color television displays and phosphors, among other applications. [1,2]

The significance of rare earths has grown significantly over the course of several decades, going well beyond the field of luminescence. The exceptional magnetic, catalytic, and electrical qualities that they possess have enabled them to become indispensable components in a wide variety of contemporary technologies. As the need for rare earths increases across all sectors of the economy, there is a growing sense of urgency to acquire a more in-depth comprehension of the electrical transitions that occur in these elements. Because of this, sophisticated analytical instruments are required, and spectroscopy stands out as a guiding light that can decipher the precise nuances of these transitions. [3,4]

The electronic structure of rare earth elements is defined by the filling of 4f orbitals, which results in a unique set of electronic configurations for each element. This is referred to as the electronic complexity of rare earths. The shielding effects and the shrinking of the energy gap between 4f orbitals are the causes of this complexity. As a consequence, a succession of absorption and emission bands that are distinct and well-defined have been produced. The different optical and magnetic properties that rare earths display are a result of the differences in the energy levels that occur throughout these transitions. [5]

When it comes to maximizing the potential of rare earths in technological applications, having a solid understanding of the electronic transitions that occur within the 4f orbitals is absolutely essential. The selection rules that govern these transitions, which are impacted by the one-of-a-kind quantum mechanical features of the 4f electrons, frequently make direct observation difficult to accomplish. When it comes to deciphering the electronic intricacies that are inherent in rare earth elements, spectroscopy emerges as a crucial instrument due to its capacity to investigate electronic transitions at both the

atomic and molecular levels. This review includes a comprehensive investigation into the many different spectroscopic techniques that are utilized in the research of rare earths. Researchers are able to analyze the transitions between energy levels through the use of absorption spectroscopy, which is a foundational method. This method provides insights into the electrical structure of rare earth elements. The emission properties of rare earth compounds can be better understood by the use of luminescence spectroscopy, which includes photoluminescence and cathodoluminescence [6,7]. This technique reveals information on the excited states and energy transfer pathways that are present inside these compounds. In addition, the field of magnetic resonance spectroscopy, which includes both nuclear magnetic resonance (NMR) and electron paramagnetic resonance (EPR), is an essential component in the process of comprehending the magnetic characteristics of particular rare earths. The use of these approaches enables researchers to investigate the interactions that occur between rare earth ions and the environment in which they are located. This provides essential information that can be utilized in the fields of magnetic materials and medical imaging.

This review also discusses developing spectroscopic techniques, such as time-resolved spectroscopy and synchrotron-based spectroscopy. It highlights the contributions that these techniques have made to the study of rare earth transitions, particularly with regard to capturing transient electronic states and offering resolution that has never been seen before. The review places an emphasis on the practical consequences of the insights acquired from these techniques as we continue our journey through the spectroscopic adventure. Through the presentation of case studies and examples, the article demonstrates how spectroscopy has played a role in the creation and optimization of materials that contain rare earths. There is a tangible connection between spectroscopic investigations and technical breakthroughs, which is provided by the exploration of applications in luminous materials, catalysts, magnetic devices, and quantum technologies. Not only does the discovery of various transitions within rare earths through the use of spectroscopy improve our fundamental understanding of these elements, but it also provides a road map for adapting the properties of these elements to specific uses. The review highlights the function that spectroscopy plays as a guiding light, shedding light on the path that leads to the full potential of rare earths being harnessed in the ever-changing landscape of modern technologies.

"Shedding Light on Rare Earths: A Spectroscopic Odyssey into Diverse Transitions" extends an invitation to researchers, scientists, and enthusiasts to embark on a journey of inquiry that will continue indefinitely. Spectroscopic interventions into the electronic transitions of rare earth elements are discussed in this review, which offers the groundwork for comprehending the past, present, and future scenarios of these interventions. The scientific community is inspired to push the boundaries of knowledge and illuminate new frontiers in the spectroscopic journey of rare earths as we stand at the convergence of scientific inquiry and technological innovation. The cry for further investigation resonates as we stand here at this intersection.

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## 2. Spectroscopy of Rare Earth Elements

The RE ion, when incorporated into a glass host, functions as an optically active center when exposed to a suitable excitation source. This occurs through the substitution of host ions, resulting in photoluminescence during this state. In this field of study, researchers commonly rely on either crystal field theory or ligand field theory as theoretical frameworks, with the choice contingent upon whether the host material exhibits a periodic lattice structure. While the solid matrix may contain RE ions, their presence could manifest in the form of either RE<sup>2+</sup> or RE<sup>3+</sup>. Both scenarios are feasible to a certain extent, and the specific form is dictated by the electronic configuration of the ions. This configuration may be either 4f n 5s25p6 or 4f n 5d5s25p6, depending on the circumstances. The determination of the exact form hinges on the electronic configuration. For instance, Xenon, with a core electronic configuration of [Xe] 4f n, serves as an exemplar of a trivalent lanthanide ion that exhibits evidence of additional 4f n electrons. [8-10]

In this research, we delve into the valences, ground states, and electronic configurations of lanthanide ions. To provide a concise overview, Table 1 presents a tabular representation of the electronic structures, valences, and ground state configurations specifically for RE<sup>3+</sup> ions.

Understanding the filling of 4f shells involves the application of Hund's rule. According to this criterion, the word exhibiting the least energy corresponds to the highest quantum number S, as larger quantum numbers signify more stable states. When multiple terms share the same quantum number S, the one with the highest angular momentum quantum number L is associated with the lowest energy. This is due to the increased accuracy in measuring angular momentum as it aligns with its magnitude. An additional point of interest is the decomposition of the designation 2S1L into levels (2S+1)LJ, where J equals L + S, L + (S-1)2, and |L S|. This decomposition highlights the versatility of the designation, influenced by spin-orbit coupling. The ground states of each ion, along with the number of 2S1L multiplets and 2S1LJ states corresponding to those ground states, are detailed in Table 1.

Efficient shielding of 4f electrons by 5s and 5p electrons in rare earth elements contributes to the consistent chemical properties of these elements. This is evident in the components themselves, with 4f 0, 4f 7, and 4f 14 representing empty, half-filled, and fully filled f shells, respectively. The valence states of lanthanides encompass various combinations, including trivalent, divalent, and tetravalent valence levels. Components such as Ce<sup>4+</sup> (4f 0), Sm<sup>2+</sup> (4f 6), Eu<sup>2+</sup> and Tb<sup>4+</sup> (4f 7), and Yb<sup>2+</sup> (4f 14) make up this group, and Table 1.1 displays the associated valence values.

Table 1: As shown the values of "n" increase in an orderly fashion, starting at 0 for La3+ and going all the way up to 14 for Lu3+.

Rare earth element	number	Neutral atom	Possible	Trivalent atom	
		electronic configuration	valence state	Electronic configuration	ground state
Lanthanum (La)	57	[Xe]4f <sup>0</sup> 5d <sup>1</sup> 6s <sup>2</sup>	3	[Xe] 4f <sup>0</sup>	<sup>1</sup> S <sub>0</sub>
Cerium(Ce)	58	[Xe]4f <sup>1</sup> 6s <sup>2</sup>	3,4	[Xe]4f <sup>1</sup>	<sup>2</sup> F <sub>3/2</sub>
Praseodymium(Pr)	59	[Xe]4f <sup>2</sup> 6s <sup>2</sup>	3,4	[Xe]4f <sup>2</sup>	<sup>3</sup> H <sub>4</sub>
Neodymium(Nd)	60	[Xe]4f <sup>3</sup> 6s <sup>2</sup>	2,3	[Xe]4f <sup>3</sup>	<sup>4</sup> I <sub>9/2</sub>
Promethium(Pm)	61	[Xe]4f <sup>4</sup> 6s <sup>2</sup>	3	[Xe]4f <sup>4</sup>	<sup>5</sup> I <sub>4</sub>
Samarium(Sm)	62	[Xe]4f <sup>6</sup> 6s <sup>2</sup>	2,3	[Xe]4f <sup>6</sup>	<sup>6</sup> H <sub>5/2</sub>
Europium(Eu)	63	[Xe] 4f <sup>7</sup> 6s <sup>2</sup>	2,3	[Xe]4f <sup>6</sup>	<sup>7</sup> F <sub>9</sub>
Gadolinium(Gd)	64	[Xe] 4f <sup>7</sup> 5d <sup>1</sup> 6s <sup>2</sup>	3	[Xe]4f <sup>7</sup>	<sup>8</sup> S <sub>7/2</sub>
Terbium(Tb)	65	[Xe] 4f <sup>9</sup> 6s <sup>2</sup>	3,4	[Xe] 4f <sup>8</sup>	<sup>7</sup> F <sub>8</sub>
Dysprosium(Dy)	66	[Xe] 4f <sup>10</sup> 6s <sup>2</sup>	3,4	[Xe] 4f <sup>9</sup>	<sup>6</sup> H <sub>15/2</sub>
Holmium(Ho)	67	[Xe] 4f <sup>11</sup> 6s <sup>2</sup>	3	[Xe]4f <sup>10</sup>	<sup>5</sup> I <sub>8</sub>
Erbium(Er)	68	[Xe] 4f <sup>12</sup> 6s <sup>2</sup>	3	[Xe] 4f <sup>11</sup>	<sup>4</sup> I <sub>13/2</sub>
Thulium(Tm)	69	[Xe] 4f <sup>13</sup> 6s <sup>2</sup>	2,3	[Xe] 4f <sup>12</sup>	<sup>3</sup> H <sub>6</sub>
Ytterbium(Yb)	70	[Xe] 4f <sup>14</sup> 6s <sup>2</sup>	2,3	[Xe] 4f <sup>13</sup>	<sup>2</sup> F <sub>7/2</sub>
Lutetium(Lu)	71	[Xe] 4f <sup>14</sup> 5d <sup>1</sup> 6s <sup>2</sup>	3	[Xe]4f <sup>14</sup>	<sup>1</sup> S <sub>0</sub>

The number of electrons within the 4f shell of lanthanide ions varies significantly among different ions. This variability arises because the number of electrons in this shell is not fixed. While the 4f n configuration is used to represent the electrical system in its ground state, the notation 4f n-15d describes the system in its first excited state. The presence of fully filled 5s2 and 5p6 orbitals shields the 4f orbitals from changes in ligands directly adjacent to them, owing to their complete filling. The unique optical properties of RE ions can be attributed to the shielding of 4f orbitals from harmful radiation.

Dieke's research group at Johns Hopkins University successfully determined the energy levels of each RE3+ ion in anhydrous trichloride. Figure 1 illustrates that RE3+ ions possess multiple energy levels, each corresponding to a distinct transition. This aligns with the observation that RE3+ ions exhibit various energy levels. Establishing the positions of J states for RE3+ ions is simpler due to minimal variations in the centers of gravity of J manifolds when interacting with the host. This finding underscores the stability of J manifolds' centers of gravity in this context.

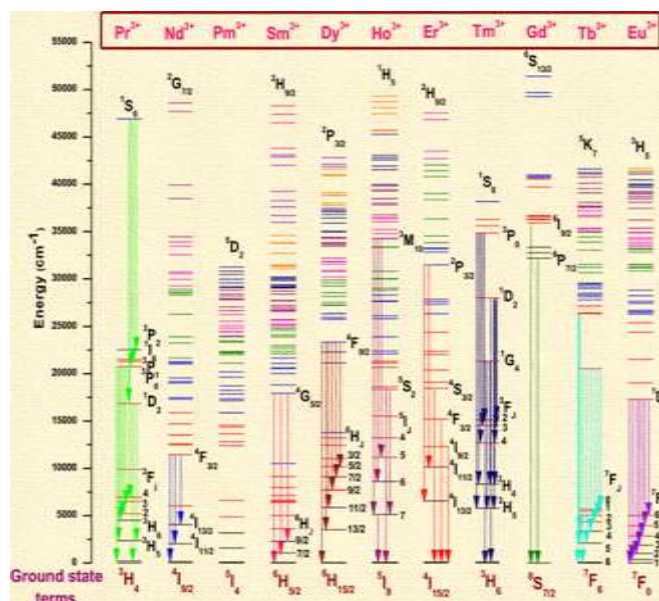


Figure 1. Shows the emission transitions and energy levels of trivalent lanthanide ions are in a schematic form

Trivalent rare earth ions have emerged as predominant activators for several reasons, outlined as follows:

The emitted light from these entities appears as diminutive lines with minimal color saturation.

In the context of the material's f-f transitions, the lengths of intra-configurational f-f transitions consistently maintain uniformity. Furthermore, their emission durations are notably extended, and they exhibit a diverse array of fluorescing states across all 4f electronic configurations, spanning a broad spectrum of wavelengths.

Analyzing slight fluctuations in the energy levels of unbound ions allows for the investigation of local fields present in glasses. Employing well-established theoretical models is a method for obtaining precise predictions of excited state dynamics and gaining a deeper understanding of how these dynamics operate. These models meticulously analyze the energies in play and the intensities of the transitions.

Trivalent lanthanide ions find frequent application in the development of optically pumped solid-state lasers. This preference stems from the exceptional quantum efficiency exhibited by trivalent lanthanide ions across a wide electromagnetic spectrum, coupled with their adequate absorption bands and distinctive emission lines, providing a comprehensive understanding of their functional dynamics.

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### 3. Transition mechanisms of rare earth ions

#### 3.1 Intra configurational f-f shifts

The phenomenon referred to as intraconfigurational f-f shifts is a notable aspect in the study of systems doped with RE<sup>3+</sup> ions, effectively examined through both absorption spectroscopy and photoluminescence spectroscopy. These spectroscopic methods prove valuable for identifying the intrinsic frequencies of doped ions, with absorption spectroscopy being a widely utilized technique in current research. When investigating systems involving RE<sup>3+</sup> ions, these approaches are universally acknowledged as highly beneficial. In the absorption spectra of RE<sup>3+</sup>-doped salts and single crystals, a distinct pattern of thin lines emerges, applicable in various scenarios. In solutions or glasses containing RE<sup>3+</sup> ions, all lines within a group exhibit a single absorption band with increased spacing between lines. The merging of these bands and lines becomes crucial for elucidating the electrical transitions within the 4f shell.

Representing the energy difference between two distinct levels of free ions with a quantum number of  $2S+1LJ$ , bands are employed to express these differences. These shifts in configuration, termed "intra-configurational transitions," define the processes within the 4f shell. A term denoted as  $2S+1LJ$ , with a degeneracy of  $2J+1$ , may split into two  $J+1$  Stark sub-levels in the presence of a sufficiently strong crystal field and symmetrical conditions. However, this splitting is contingent upon the symmetry of the crystal field. The number of distinguishable Stark components becomes a tool for comprehending the symmetry of the crystal field. Despite the influence of the crystal field on the energies of free ions being potentially dismissed as unimportant, the splitting caused by 4f electrons remains of low significance, leading to inconsequential changes in spectra across various matrices.

The method based on the number of free ions proved effective in detecting nearly all spectral lines. The distinctive luminous features exhibited by RE ions stem from transitions within levels generated from partially occupied 4f n electronic subshells, responsible for light emission. However, perturbation effects induced by ligand fields allow these transitions under certain conditions, despite the Laporte selection rule stating they cannot occur in free ions, except in specific situations [11].

#### 3.2 The induced electric-dipole transitions

Interaction between an electric dipole and the electric field vector of electromagnetic radiation occurs when a spectroscopically active ion, like the Ln<sup>3+</sup> ion, forms an electric dipole transition (ED). Paradox allows electric-dipole (ED) transitions to take place between the 4f and 5d configuration states. The oscillator strengths of f-d transitions are substantially larger than those of f-f transitions, which typically range from 10<sup>1</sup> to 10<sup>2</sup> MHz in frequency. To choose individuals for the ED transition, we will employ the following criteria: While  $J=0$  or  $J=6$ ,  $l=1$ ,  $\Delta r=0$ ,  $S=0$ ,  $L=6$ , and  $J=6$ ,  $J=2,4$ , or 6 otherwise. Making an electric dipole causes charges to move in an odd-parity direction in a linear fashion. As per the Laporte selection criteria, the intraconfigurational electric dipole transitions are not permitted. Nevertheless, the f-f electric dipole (ED) transitions are prevented from happening when the 4f n configuration is present alongside an excited configuration of opposite parity, such as 4f n-1 5d. Two electronic states with opposite parities can merge into one under the influence of non-centrosymmetric interactions. Typically, the transitions mentioned above are referred to as induced ED transitions, and their intensities typically hover around 10<sup>-6</sup>. The observed transitions were significantly weaker than the typical electric dipole transitions. The intensities of the ED transitions that were achieved might be explained by the Judd-Ofelt (J-O) theory [12,13].

#### 3.3 Transitions Involving Magnetic Dipoles

Within the framework of the Russell-Saunders limit, it is possible for magnetic dipole (MD) transitions to occur between the 4f n states. Certain selection criteria, however, must be achieved before these transitions can be approved. To be more precise, changes that involve a parity change of 0 are not permitted during transitions. Similarly, transitions where the sum of the angular momentum of the orbits (L) or the spins (S) is zero are not allowed. Also not included are transitions where  $J=0$ , the whole angular momentum. Magnetic dipole transitions are generated when a spectroscopically active ion, specifically the Ln<sup>3+</sup> ion, interacts with the magnetic field component of light. The intensities of MD transitions are approximately 10<sup>-8</sup> times weaker than the intensities of induced electric dipole transitions.

#### 3.4 Transitions of Electric Quadrupole Fields

The displacement of a charge with quadrupole characteristics can lead to electric quadrupole transitions. S, L, and J are the selection criteria for 4f n states/transitions [14,15]: they must all be smaller than zero, two, and two, respectively. A pseudo-quadrupole transition is a name for a hypersensitive

transition since it follows the same selection criteria as a quadrupole transition. Hypersensitive transitions, however, are far less harsh than contrived ED and MD transitions, you must remember this. Evidence for the quadrupole transition in lanthanide spectra is currently lacking in the empirical literature.

### 3.5 Hypersensitive transition

A unique property of RE ion absorption bands is their extreme sensitivity to their host environment. The term for these changes is hypersensitive transitions. The selection criteria for this type of transition are that  $S$  is less than zero,  $L$  is greater than two, and  $J$  is greater than two. The presence of an uneven ligand environment surrounding the rare earth ion could be associated with the heightened sensitivity of the absorption transition, as suggested by Jorgensen and Judd [16]. Their investigation into the rare earth ion's habitat led them to this verdict. It is also possible that polarizability influences the sensitivity of transitions. Greater values of the reduced matrix components, especially  $\|U_2\|$ , may aid the hypersensitive transitions, as seen by Judd and Ofelt. The fact that this was noticed proves it. By analyzing the variation of its  $2 J-O$  parameter in different host matrices, one can determine the hypersensitivity level shown by a rare earth (RE) ion. Several methods exist for accomplishing this. The unusual hypersensitive transition fluctuations can be explained by the ubiquitous coordination and symmetry surrounding the lanthanide ion. One potential qualitative indicator for determining a site's symmetry could be the examination of the band structure and intensity of hypersensitive transitions [17,18]. A spectrometer could be used to do this investigation.

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## 5. Conclusion

In conclusion, the study delves into the intricate realm of spectroscopy concerning RE, particularly the incorporation of RE ions into a glass host. The RE ions serve as optically active centers when exposed to suitable excitation sources, operating by substituting host ions and inducing photoluminescence in this state. The theoretical foundations for such studies revolve around crystal field theory or ligand field theory, with the choice contingent upon the periodic lattice structure of the host material. The investigation further explores the valences, ground states, and electronic configurations of lanthanide ions, employing Hund's rule for understanding the filling of 4f shells. The systematic representation in Table 1 offers a comprehensive overview of electronic structures, valences, and ground state configurations specifically for RE<sup>3+</sup> ions. The shielding effect of 5s and 5p electrons on 4f electrons in rare earth elements contributes to their consistent chemical properties. The research sheds light on the variability in the number of electrons within the 4f shell of lanthanide ions and the shielding impact of fully filled 5s<sup>2</sup> and 5p<sup>6</sup> orbitals. Dieke's work at Johns Hopkins University successfully determined the energy levels of each RE<sup>3+</sup> ion in anhydrous trichloride, revealing multiple energy levels corresponding to distinct transitions. Transition mechanisms, such as intraconfigurational f-f shifts, induced electric-dipole transitions, magnetic dipole transitions, and electric quadrupole transitions, are discussed. The study highlights the unique properties of RE ions, their utilization in optically pumped solid-state lasers, and the importance of understanding their transition dynamics for various applications. The investigation into hypersensitive transitions emphasizes the sensitivity of RE ion absorption bands to their host environment, providing potential qualitative metrics for determining site symmetry. Overall, this comprehensive exploration contributes valuable insights into the spectroscopy of Rare Earth Elements, offering a foundation for further research and practical applications in diverse fields.

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